## **Supplementary material**

The adiabatic passage pulse sequences used in these experiments are shown below in the figure. They follow a similar for to those used in reference 2 and 4. (a) corresponds to the pulse sequence applied to the microwire source during normal MRFM measurements including those shown in Fig. 3 of the paper.  $T_c$  is the period of the cantilever and corresponds in the text to  $T_c = 2\pi/\omega_m = 385 \,\mu\text{s}$  in the text.  $v_{RF}$  is the carrier frequency of the pulses and is swept in Fig. 3, for example.  $\Delta v = \Omega_{RF}/(2\pi)$  is the modulation width, which in these experiments is 600 kHz. *a* and *b* are amplitude modulation parameters which in these experiments were set to a = 0.2 and b = 0.5.  $B_I$  is the magnitude of the rotating magnetic field produced at the sample by the microwire. In the case of our experiments  $B_I = 12 \,\text{mT}$  as demonstrated in the nutation experiment of Fig. 5. (b) corresponds to the pulse sequence used for the nutation experiment plotted in Fig. 5. Here  $T_p = 500 \times T_c = 190 \,\text{ms}$  is the repetition rate of the variable length pulse. The length of the pulse is given by  $\tau_p$  and is swept in Fig. 5, for example.





## Table I

FeCo tip parameters	
Geometry	Truncated cone magnetized along the z-direction
Apex diameter	270 nm
Base diameter	510 nm
Height	250 nm
Saturation magnetization	$10^{6} \text{ A/m}$
Polystyrene sample parameters	
Geometry	Sphere
Radius	625 nm
<sup>1</sup> H density	$4.9 \times 10^{22} \text{ cm}^{-3}$

**Figure 2** Scanning Electron Microscope image of cantilever with polystyrene attached similar to the one measured in the experiments presented:

