

Basics

Ohm's Law :

$$V = I R$$

voltage
 $[V = \frac{J}{C}]$

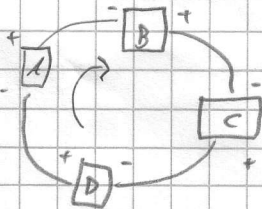
current
 $[A = \frac{C}{s}]$

resistance
 $[\Omega = \frac{V}{A} = \frac{J \cdot s}{C^2}]$

Kirchhoff's Laws :

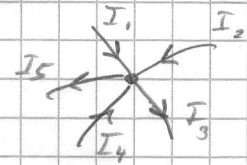
Sum of voltages around a loop is zero.

(conservation of energy)



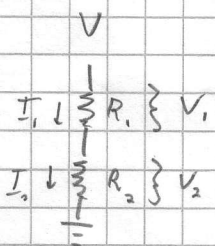
Sum of currents in and out of a node is zero.

(conservation of charge)



Applications

Series



$$I_{total} = I_1 = I_2$$

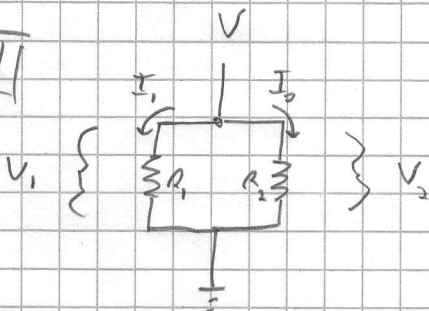
$$V_{total} = V_1 + V_2$$

$$V_{total} = I_1 R_1 + I_2 R_2 = I_{total} (R_1 + R_2)$$

$$V_{total} = I_{total} R_{total}$$

$$\rightarrow (R_1 + R_2)$$

parallel



$$I_{total} = I_1 + I_2$$

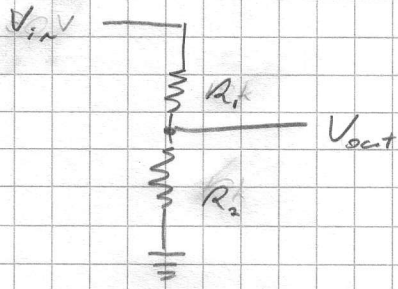
$$V_{total} = V_1 = V_2$$

$$I_{total} = \frac{V_1}{R_1} + \frac{V_2}{R_2} = V_{total} \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$V_{total} = I_{total} R_{total}$$

$$\rightarrow \left(\frac{R_1 R_2}{R_1 + R_2} \right)$$

Voltage Divider

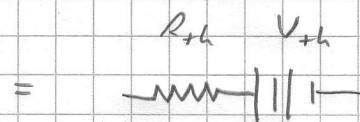
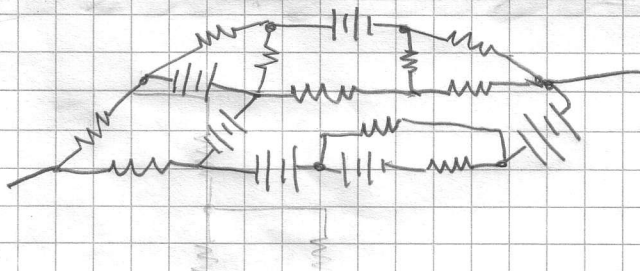


Method 1: $I = \frac{V_{in}}{R_1 + R_2}$

$V_{out} = I \cdot R_2$

Method 2: $V_{out} = V_{in} \left(\frac{R_2}{R_1 + R_2} \right)$

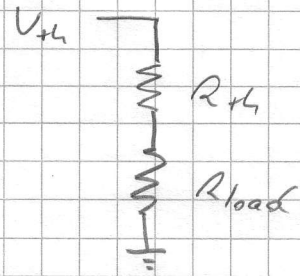
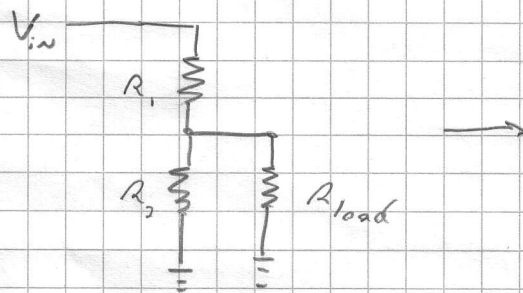
Thevenin's Equivalent Circuit



$V_{th} = V \text{ (open circuit)}$

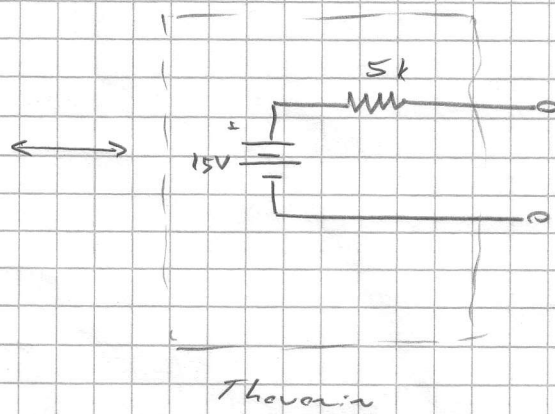
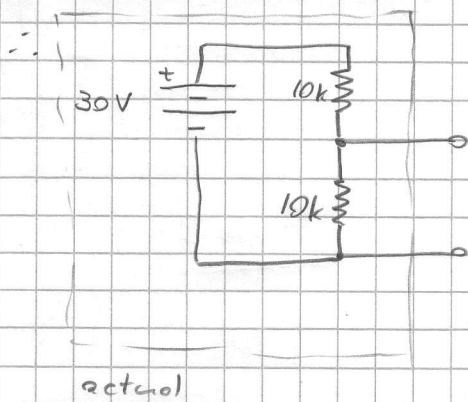
$R_{th} = \frac{V \text{ (open circuit)}}{I \text{ (short circuit)}}$

Example:



$V_{th} = V_{in} \frac{R_2}{R_1 + R_2}$

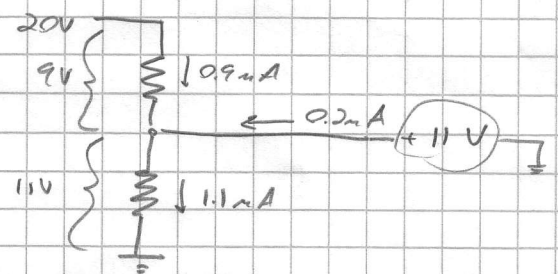
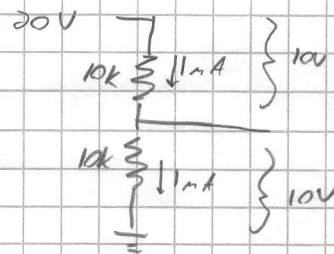
$R_{th} = \frac{V_{in} \left(\frac{R_2}{R_1 + R_2} \right)}{\frac{V_{in}}{R_1}} = \frac{R_1 R_2}{R_1 + R_2}$



Short cut for calculating R_{th} :

R_{th} is the parallel resistance of the several resistances viewed from the output.

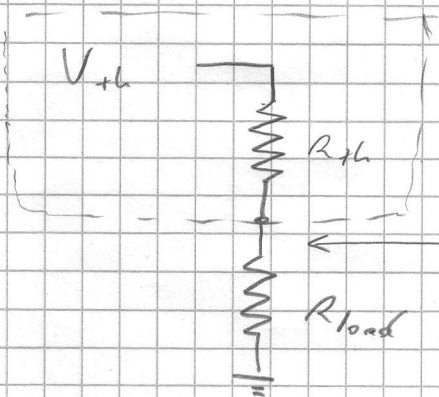
Example



$$\frac{\Delta V}{\Delta A} = \frac{1V}{0.2mA} = 5k\Omega \leftarrow R_{th}$$

To find impedance at a point, find ΔV & ΔA at that point.

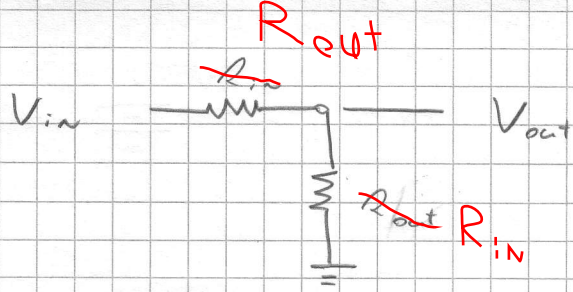
Input & Output Impedance



$$V_{out} = V_{th} \frac{R_{load}}{R_{th} + R_{load}}$$

$$V_{out} \approx V_{th} \quad \text{for} \quad R_{load} \gg R_{th}$$

$$V_{out} \rightarrow 0 \quad \text{for} \quad R_{load} \ll R_{th}$$

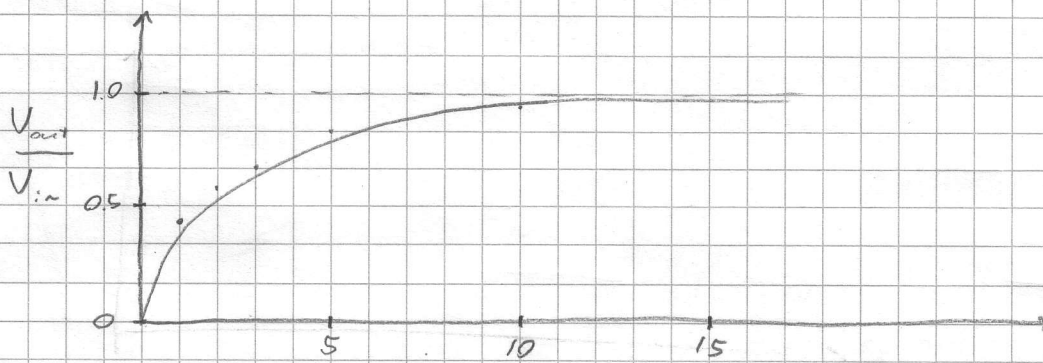


Always design
such that

$R_{out} \ll R_{in}$

↑
output impedance
(From load)

↑
input impedance
(From instrument)



~~$\frac{R_{out}}{R_{in}}$~~ $\frac{R_{in}}{R_{out}}$