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Exercises and Complements for the Introduction to Physics I  
for Students  
of Biology, Pharmacy and Geoscience

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Sheet 1 / 12.09.2017

Discussion of the Exercises: **26.09.2017/27.09.2017**

**Exercise 1.**

Find the derivative  $dy/dx$  of the following functions:

(a)  $y(x) = ax^3 + bx^2 + cx + d$

(c)  $y(x) = x \exp^{-ax}$

(b)  $y(x) = b \ln(ax)$

(d)  $y(x) = ax\sqrt{1 - bx^3}$

Find the derivative of the following functions with respect to time  $t$ :

(a)  $E(t) = \frac{1}{2}mv^2(t)$

(b)  $p(t) = mv(t)$

Calculate the integral  $F(x) = \int f(x)dx$  of the following functions:

(a)  $f(x) = 3x^3 + 2x^2$

(b)  $f(x) = a \sin(bx)$

(c)  $f(x) = \frac{4}{x}$

Given the vectors  $\vec{a} = \begin{pmatrix} 1 \\ 3 \\ -4 \end{pmatrix}$  and  $\vec{b} = \begin{pmatrix} 3 \\ 5 \\ -1 \end{pmatrix}$ , calculate the following vectors:

(a)  $\vec{s} = \vec{a} + \vec{b}$       (c)  $\vec{c} = \vec{a} \times \vec{b}$

(b)  $\vec{s} = \vec{a} - \vec{b}$       (d)  $c = \vec{a} \cdot \vec{b}$

Solve (a) and (b) graphically in the  $xy$ -plane.

### Exercise 2.

Determine the SI units of the two constants  $C_1$  and  $C_2$  ( $x$ [m],  $t$ [s],  $v$ [m/s],  $F$ [N],  $m_1$ [kg],  $m_2$ [kg]).

(a)  $x = C_1 + C_2 t$

(d)  $F = C_1 \frac{m_1 m_2}{x^2}$

(b)  $v^2 = 2C_1 x$

(e)  $v = C_1 \exp(x/C_2)$

(c)  $v = C_1 x \ln(C_2 t)$

### Exercise 3.

Light propagates in vacuum with a constant speed of  $3 \cdot 10^8$  m/s.

(a) How long does light need to travel a distance equal to the diameter of the nucleus of a H-atom ( $10^{-15}$  m)?

(b) How long does light need to travel from the Sun to the Earth (calculate in s and min)? The distance between Sun and Earth is referred to as astronomical unit:  $1 \text{ AU} = 1.5 \cdot 10^8$  km.

(c) How long does light need to cross the solar system with a diameter of  $1.2 \cdot 10^{10}$  km?

### Exercise 4.

The ride of a car between one traffic light to the next one is observed and studied. The vehicle is uniformly accelerated from a standstill for a period of 6 s with  $2.1 \text{ m/s}^2$ . The car continues with this acquired velocity for 5 s. It stops at the next traffic light due to a deceleration (negative acceleration) of  $4.2 \text{ m/s}^2$ .

(a) What is the the maximum velocity which the car reaches (in km/h)?

(b) Which distance does the car cover during the acceleration?

(c) How far does the car drive with a constant velocity?

(d) Calculate the stopping distance.

(e) How long is the total distance between the two traffic lights?

### Exercise 5.

Tell for each of the four  $x(t)$ -curves in the following figures, if:

(a) the velocity at the time  $t_2$  is greater, less or equal than at the time  $t_1$ .

(b) the absolute value of the velocity at the time  $t_2$  is greater, less or equal than the absolute value at the time  $t_1$ .

